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## An Iterative Channel Estimation and Decoding Algorithm for CDMA Systems in Uplink Environments

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LDPC CDMA  
LDPC

I.

Liu 가

가  
Wideband CDMA  
(W-CDMA) [1], cdma2000 [2]  
(CDMA)

가 Data-aided [3]-[5]. [3]

Data-aided (LDPC) 가 II III IV V

[6]-[9]. II.  
(Factor graph) [6] [8][9] 가  
(Kalman) [9] (Wiener) 가

$$r(l, m, k) = \sqrt{P} \{ X(l, m) C_D(k) + \lambda C_P(m, k) \} h(l) + n(l, m, k), \quad (1)$$

1 AR Liu 가 [9]

$$r(l, m, k) = \sqrt{P} \{ X(l, m) C_D(k) + \lambda C_P(m, k) \} h(l) + n(l, m, k), \quad (1)$$



$$\begin{aligned}
Z_r^{(q)} &= y_D(l, m) h_K^*(l) \\
&= \sqrt{P} X(l, m) h(l) h_K^*(l) \\
&\quad + \frac{1}{SF_D} \sum_{k=0}^{SF_D-1} n(l, m, k) C_D(k) h_K^*(l) \\
&= \frac{X(l, m)}{\lambda} \tilde{h}(l) h_K^*(l) \\
&\quad + \frac{1}{SF_D} \sum_{k=0}^{SF_D-1} n(l, m, k) C_D(k) h_K^*(l) \\
&\approx \frac{X(l, m)}{\lambda} \left| \tilde{h}(l) \right|^2 + h_K^*(l) n_D(l, m) \\
&\quad + \frac{1}{\lambda} X(l, m) \tilde{h}(l) e_h^*(l). \tag{7}
\end{aligned}$$

$$e_h(l) = \tilde{h}(l) - h_K(l) \tag{8}$$

$$\begin{aligned}
LLR(l, m) &= -\frac{\left( Z_r^{(q)}(l, m) - |h_K(l)|^2 / 2\lambda \right)^2}{2\sigma^2} \\
&\quad + \frac{\left( Z_r^{(q)}(l, m) + |h_K(l)|^2 / 2\lambda \right)^2}{2\sigma^2} \\
&= \frac{2Z_r^{(q)}(l, m) |h_K(l)|^2 / 2\lambda}{\sigma^2} \\
&= \frac{\sqrt{2} |h_K(l)|^2 Z_r^{(q)}(l, m) / \lambda}{|h_K(l)|^2 \sigma_n^2 / SF_D + |h_K(l)|^2 \sigma_e^2 / 2\lambda^2} \\
&= \frac{\sqrt{2} Z_r^{(q)}(l, m)}{\lambda \left( \sigma_n^2 / SF_D + \sigma_e^2 / 2\lambda^2 \right)}, \tag{8}
\end{aligned}$$

$$y_D(l, m) = \frac{1}{\lambda} X(l, m) \tilde{h}(l) + n_D(l, m). \tag{9}$$

$$y_{D,v}(l, m) = \frac{1}{\lambda} X(l, m) \tilde{h}(l) + n_{D,v}(l, m). \tag{9}$$

$$\begin{aligned}
h_{D,v}(l, m) &= y_{D,v}(l, m) \lambda \\
&= \frac{X(l, m)}{S_v} \tilde{h}(l) + \frac{\lambda}{S_v} n_{D,v}(l, m), \tag{10}
\end{aligned}$$

$$\begin{aligned}
\tilde{h}_D(l, m) &= \sum_{v=0}^3 P_v(l, m) h_{D,v}(l, m). \tag{11}
\end{aligned}$$

$$\begin{aligned}
P_v(l, m) &= \arg \max_v p_v(l, m), \tag{12} \\
v^-(l, m) &= (v^+(l, m) + 1) \bmod 4, \tag{13} \\
X(l, m) &= S_{v^+(l, m)}, \tag{14} \\
\tilde{h}_D(l, m) &= \left( P_{v^+(l, m)} - \bar{P}_{v^+(l, m)} \right) \tilde{h}(l) + \left( P_{v^-(l, m)} - \bar{P}_{v^-(l, m)} \right) j \tilde{h}(l) \\
&\quad + n_D(l, m) \lambda \bar{S}^*(l, m), \tag{15}
\end{aligned}$$

$$v^+(l, m) = \arg \max_v p_v(l, m), \tag{12}$$

$$v^-(l, m) = (v^+(l, m) + 1) \bmod 4, \tag{13}$$

$$X(l, m) = S_{v^+(l, m)}, \tag{14}$$

$$\tilde{h}_D(l, m) = \left( P_{v^+(l, m)} - \bar{P}_{v^+(l, m)} \right) \tilde{h}(l) + \left( P_{v^-(l, m)} - \bar{P}_{v^-(l, m)} \right) j \tilde{h}(l) + n_D(l, m) \lambda \bar{S}^*(l, m), \tag{15}$$

$$\bar{S}(l, m) = \bar{P}_{v(l, m)} \tag{15}$$

$$\tilde{h}_D(l, m) = \frac{1}{P(l, m)} \tilde{h}_D(l, m)$$

$$= \tilde{h}(l) + \frac{P^\perp(l, m)}{P(l, m)} j \tilde{h}(l) + \frac{\lambda_{D,P}}{P(l, m)} \bar{S}^*(l, m) n_D(l, m), \tag{16}$$

$$P(l, m) = P_{v^+(l, m)} - \bar{P}_{v^+(l, m)}, \quad P^\perp(l, m) = P_{v^-(l, m)} - \bar{P}_{v^-(l, m)}$$

$$\tilde{h}_D(l, m) = \tilde{h}(l) + \frac{\lambda_{D,P}}{P(l, m)} \bar{S}^*(l, m) n_D(l, m)$$

$$q_D(l, m) \triangleq E \left\{ \left| \tilde{h}_D(l, m) - \tilde{h}(l) \right|^2 \right\}$$

$$= \left[ \frac{P^\perp(l, m)}{P(l, m)} \right]^2 \left| \tilde{h}(l) \right|^2 + \frac{\lambda^2 \left| \bar{S}(l, m) \right|^2 \sigma_n^2}{P^2(l, m) SF_D}$$

$$\approx \left[ \frac{P^\perp(l, m)}{P(l, m)} \right]^2 \left| h_K(l) \right|^2 + \frac{\lambda^2 \left| \bar{S}(l, m) \right|^2 \sigma_n^2}{P^2(l, m) SF_D} \tag{17}$$

$$\begin{aligned}
q_p(l) &= \frac{1}{S_v} \tag{18} \\
q_r(l) &= \frac{1}{S_v} \tag{18}
\end{aligned}$$

$$\bar{y}_c(l) = \left( \frac{y_p(l)}{q_p(l)} + \sum_{m=0}^{\gamma-1} \frac{\tilde{h}_D(l,m)}{q_D(l,m)} \right) / \left( \frac{1}{q_p(l)} + \sum_{m=0}^{\gamma-1} \frac{1}{q_D(l,m)} \right) \quad (18)$$

$$= \tilde{h}(l) + \bar{n}_c(l)$$

$$\text{Var}\{\bar{y}_c(l)\} = \left( \frac{1}{q_p(l)} + \sum_{m=0}^{\gamma-1} \frac{1}{q_D(l,m)} \right)^{-1} \quad (19)$$

$$\frac{\text{Var}\{\bar{y}_c(l)\}}{\bar{y}_c(l)}$$

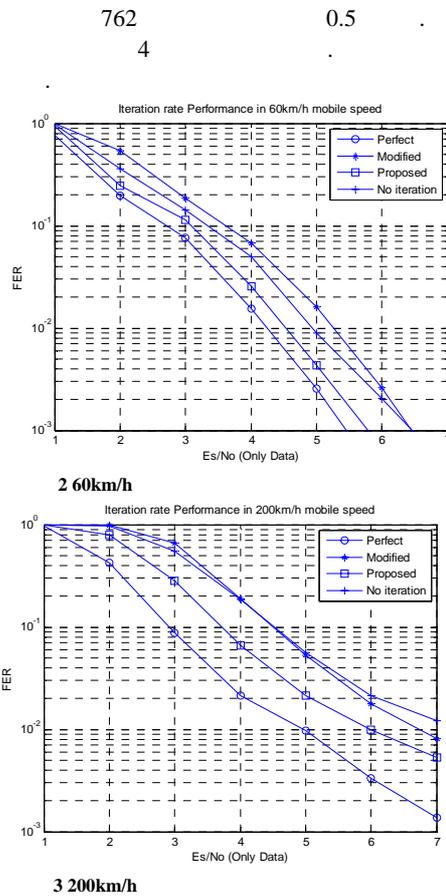
(7)  $h_K(l)$   $\bar{y}_c(l)$

V.

QPSK

QPSK

IV.



‘Perfect’  
 ‘Modified reference’ Liu [9]  
 ‘Proposed’  
 ‘No Iteration’  
 LDPC  
 2, 3  
 [9]

SNR

4

SNR

가

가

QUALCOMM YONSEI CDMA Research Lab.

VI.

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